

# Consensus in Systems with Eventual Quiescence

**Brief Announcement** 

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SSS2025, October 11th, 2025

Paper: "Reaching Consensus in the Presence of Contention-Related Crash Failures" by Anaïs Durand, Michel Raynal & Gadi Taubenfeld, SSS 2022

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Algorithm solving consensus tolerating up to k  $\lambda$ -constrained crashes, when  $\lambda = n - k$ , using objects with consensus number k

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Example with n = 10 at most k = 4 crashes

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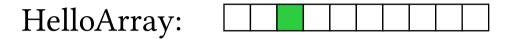
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TrustedArray:

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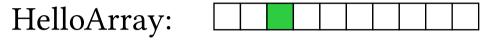


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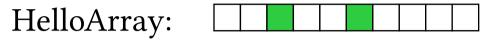


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HelloArray:  $n-3 \geq n-k$  TrustedArray:

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- Wait to see at least n k "hello"
- I know that no more crash can occur

Let 0 < k < n, we want to solve the consensus with at most  $k \pmod{n-k}$ -constrained crashes.

Example with n = 10 at most k = 4 crashes

- Say "hello" (write 1 in my "hello" register)
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## Thank you!